

Math 350  
Spring, 2000

### HOMEWORK #1

Do 50 points of the following problems (due 1/18/00).

- 15 pts.    **1** The Chemical Abstract Service uses the following scheme for registry numbers:  $a_1a_2\dots a_7$  are the identification digits, and the check digit is  $a_8 = 7 \cdot a_1 + 6 \cdot a_2 + 5 \cdot a_3 + 4 \cdot a_4 + 3 \cdot a_5 + 2 \cdot a_6 + 1 \cdot a_7 \pmod{10}$ . What mistyped digits will not be detected? What about transpositions?
- 15 pts.    **2** Generalize problem 1.5, p.10, to a 3-ary  $(k,M,2)$ -code (do parts (i) and (ii)).
- 30 pts.,  
★        **3** If you have 16 messages to send, and you want to be able to correct errors, one way to do that is to use a binary  $(12,16,3)$  repetition code. This code is created by numbering the 16 messages in binary, then repeating them 3 times while sending. Discuss the error correcting capabilities of this system (when can it correct 2 errors, 3 errors, ...)? Explain how you would do your error correcting. If each digit has a probability of .99 of being received properly and we assume that errors in digits are independent events, what is the probability that the word is received correctly?
- 20 pts.    **4** Let  $C$  be the binary code of length 6 made up of all of the codewords of even weight. What is  $M$ ? What is  $d$ ? What received words can be decoded unambiguously? What received words will give problems? What properties will this code have if it is repeated twice? How would you correct errors?